## Centro di Ricerca Matematica "Ennio De Giorgi"

Intensive research period
May - June 2010
Configuration Spaces: Geometry, Combinatorics and Topology

## Mini-courses

## Preliminary list of courses

Sergey Yuzvinsky: $A$ short introduction to arrangements of hyperplanes May 5-6, Sala Conferenze

Stefan Papadima, Alex Suciu: Cohomology jumping loci and homologicad finiteness properties - May 10-14, (for the seminar rooms see the timetable)
Sergey Yuzvinsky: Resonance varieties for arrangements and their relations to combinatorics and algebraic geometry - May 10-11, Aula Dini

Claudio Procesi: Splines and partition functions - May 17-21, (For the seminar rooms see the timetable)
Fred Cohen: Moment-angle complexes, their stable structure and cohomology - May 31-June 4, Aula Dini

Eduard Looijenga: Aspects of the KZ system - May 31-June 4, Aula Dini
Alexander Varchenko: The quantum integrable model of an arrangement of hyperplanes - June 7-11, Aula Dini

Dev Sinha: Hopf rings in topology and algebra - June 14-18, Aula Dini
Michèle Vergne: Remarks on Box splines - June 14-18, Aula Dini

| Configuration spaces: mini courses |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Timetable |  |  |  |  |
| May 2010 |  |  |  |  |
| Monday | Tuesday | Wednesday | Thursday | Friday |
| 3 | 4 | $\begin{aligned} & \hline \mathbf{5} \\ & \text { 10:30-12:00 } \\ & \text { Yuzvinsky (ConFEr.) } \\ & \text { 12:00-12:30 } \\ & \text { Welcome cocktail } \end{aligned}$ | 6 <br> 10:30 Coffee break <br> 11:00-12:30 (Confer.) <br> Yuzvinsky | 7 |
| 10 <br> 9:30-11:00 <br> Suciu (Dini) <br> 11:00 Coffee break <br> 11.15-12.45 <br> Yuzvinsky (Dini) | 11 <br> 9:30-11:00 <br> Suciu (Dini) <br> 11:00 Coffee break <br> 11.15-12.45 <br> Yuzvinsky (Dini) | 12 <br> 10:45 Coffee break <br> 11.15-12.45 <br> Papadima (Bianchi) | 13 <br> 10:45 Coffee break <br> 11.15-12.45 <br> Papadima (Dini) | 14 <br> 10:45 Coffee break <br> 11:15-12:45 <br> Suciu (Conferenze) |
| 17 <br> 10:30 Coffee break <br> 11:00-12:30 <br> Procesi (Dini) | 18 <br> 10:30 Coffee break <br> 11:00-12:30 <br> Procesi (Stemmi) | 19 | 20 <br> 9:30-11:00 <br> Procesi (Stemmi) <br> 11:00 Coffee break | 21 <br> 10:30 Coffee break <br> 11:00-12:30 <br> Procesi (Bianchi) |
| 24 | 25 | 26 | 27 | 28 |
| WORKSHOP | WORKSHOP | WORKSHOP |  |  |


| Configuration spaces: mini courses |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Timetable |  |  |  |  |
| May-June 2010 |  |  |  |  |
| Monday | Tuesday | Wednesday | Thursday | Friday |
| 31 (May) | 1 (June) | 2 | 3 | 4 |
| 9:30-11:00 | 9:30-11:00 |  | 9:30-11:00 | 9:30-11:00 |
| Cohen (Dini) | Cohen (Dini) |  | Looijenga (Dini) | Looijenga (Dini) |
| 11:00 Coffee break $11 \cdot 15-12 \cdot 45$ | 11:00 Coffee break |  | 11:00 Coffee break | 11:00 Coffee break |
| 11:15-12:45 | 11:15-12:45 | HOLIDAY | 11:15-12:45 | 11:15-12:45 |
| Looijenga (Dini) | Looijenga (Dini) |  | Cohen (Dini) | Cohen (Dini) |
| 7 | 8 | 9 | 10 | 11 |
| 10:30 Coffee break | 10:30 Coffee break | 10:30 Coffee break | 10:30 Coffee break | 10:30 Coffee break |
| 11:00-12:30 | 11:00-12:30 | 11:00-12:30 | 11:00-12:30 | 11:00-12:30 |
| Varchenko (Dinı) | Varchenko (Dini) | Varchenko (Dini) | Varchenko (Dini) | Varchenko (Dini) |
| 14 | 15 | 16 | 17 | 18 |
| 10:30 Coffee break | 9:30-11:00 | 9:30-11:00 |  | 9:30-11:00 |
| 11:00-12:30 | Vergne (Dini) | Sinha (Dini) |  | Sinha (Dini) |
| Vergne (Dini) | 11:00 Coffee break | 11:00 Coffee break |  | 11:00 Coffee break |
| 16:00-17:00 | 11:15-12:45 | 11:15-12:45 | HOLIDAY | 11:15-12:45 |
| Sinha (Dini) | Sinha (Dini) | Vergne (Dini) |  | Vergne (Dini) |
| 21 | 22 | 23 | 24 | 25 |
| WORKSHOP | WORKSHOP | WORKSHOP | WORKSHOP | WORKSHOP |

## Abstracts of the courses:

A short introduction to arrangements of hyperplanes (May 5-6, Sala Conferenze)
Sergey Yuzvinsky - University of Oregon, Eugene

> LIST OF COURSES

Cohomology jumping loci and homological finiteness properties
(May 10-14, Aula Dini)
Stefan Papadima - Institute of Mathematics "Simion Stoilow" of the Romanian Academy, Bucharest
Alex Suciu - Northeastern University, Boston

1 Homology of local systems and characteristic varieties
2 Homology of free abelian covers
3 Resonance varieties, tangent cones, formality
4 Bieri-Neumann-Strebel-Renz invariants
5 Applications:
a Knots, links, and 3-dimensional manifolds,
b Right-angled Artin groups and toric complexes,
c Kahler and quasi-Kahler manifolds,
d Hyperplane arrangements

Resonance varieties for arrangements and their relations to combinatorics and algebraic geometry
(May 10-11, Aula Dini)
Sergey Yuzvinsky - University of Oregon, Eugene

Splines and partition functions
(May 17-21, for the seminar room, see the timetable)
Claudio Procesi - Universitá "La Sapienza" Roma
LIST OF COURSES
I will discuss several constructions one can perform starting from a list of vectors and show how some ideas coming from the theory of hyperplane arrangements come into play in numerical analysis and arithmetic. The material is based on a forthcoming book with De Concini, preliminary version available at www.mat.uniroma1.it/~procesi/dida.html: Hyperplane arrangements, polytopes, box-splines.

Moment-angle complexes, their stable structure and cohomology
(May 31-June 4, Aula Dini)
Fred Cohen - University of Rochester, Rochester

Aspects of the KZ system
(May 31-June 4, Aula Dini)
Eduard Looijenga - Universiteit Utrecht
LIST OF COURSES
The goal of this minicourse is to show how this local system can be understood in algebro-geometric terms. We will also discuss certain important subsystems (known as Hitchin or $W Z W$ systems). It has been conjectured that these subsystems have a flat inner product. We will verify this, essentially following Ramadas, that this is so when one the input data (a simple Lie algebra) is $S L(2)$.

The quantum integrable model of an arrangement of hyperplanes (June 7-11, Aula Dini)
Alexander Varchenko - University of North Carolina at Chapel Hill
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Hopf rings in topology and algebra (June 14-18, Aula Dini)
Dev Sinha - University of Oregon
LIST OF COURSES
We start with some topics very close to the theme of the workshop, namely the cohomology of unordered configuration spaces and in particular of symmetric groups, as recently studied by Giusti, Salvatore and myself. A key organizing concept is that of a Hopf ring, which is a ring object in the category of coaglebras. This notion has been mostly applied in the study of homology of spaces which represent multiplicative cohomology theories such as Eilenberg--MacClane spaces or infinite Grassmannians. But we have found that this structure also applies to cohomology, representation theory, and invariant theory of finite "series groups" such as symmetric or alternating groups and general linear groups over finite fields. We both revisit some classical topics and indicate some open areas of investigation stemming from these ideas.

Remarks on Box splines
(June 14-18, Aula Dini)
Michèle Vergne - Centre National de la Recherche Scientifique Ecole Polytechnique. Centre de Mathematiques Laurent Schwartz

## Location

Most of the lectures will take place in Sala Conferenze, inside Collegio Puteano (number 2 in the map below) or in Aula Dini, inside Palazzo del Castelletto (number 1 in the map below). Some lectures will take place in Aula Bianchi or in Aula Stemmi, inside Palazzo della Carovana (number 3 in the picture). Look also at http://www.crm.sns.it/hpp/practical/maps.html.


Table 1: Map with the location of Palazzo del Castelletto (number 1), Collegio Puteano (number 2) and Palazzo della Carovana (number 3)

